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The mathematical principles of mechanical philosophy, and their application to the theory of universal gravitation

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