

www.e-rara.ch

Theoria motuum lunae nova methodo pertractata

Euler, Leonhard

Petropoli, 1772

ETH-Bibliothek Zürich

Shelf Mark: Rar 4289

Persistent Link: <https://doi.org/10.3931/e-rara-2136>

Caput IV. Evolutio aequationum ordinis $i i \kappa$ pro litteris Z et Z.

www.e-rara.ch

Die Plattform e-rara.ch macht die in Schweizer Bibliotheken vorhandenen Drucke online verfügbar. Das Spektrum reicht von Büchern über Karten bis zu illustrierten Materialien – von den Anfängen des Buchdrucks bis ins 20. Jahrhundert.

e-rara.ch provides online access to rare books available in Swiss libraries. The holdings extend from books and maps to illustrated material – from the beginnings of printing to the 20th century.

e-rara.ch met en ligne des reproductions numériques d'imprimés conservés dans les bibliothèques de Suisse. L'éventail va des livres aux documents iconographiques en passant par les cartes – des débuts de l'imprimerie jusqu'au 20e siècle.

e-rara.ch mette a disposizione in rete le edizioni antiche conservate nelle biblioteche svizzere. La collezione comprende libri, carte geografiche e materiale illustrato che risalgono agli inizi della tipografia fino ad arrivare al XX secolo.

Nutzungsbedingungen Dieses Digitalisat kann kostenfrei heruntergeladen werden. Die Lizenzierungsart und die Nutzungsbedingungen sind individuell zu jedem Dokument in den Titelinformationen angegeben. Für weitere Informationen siehe auch [Link]

Terms of Use This digital copy can be downloaded free of charge. The type of licensing and the terms of use are indicated in the title information for each document individually. For further information please refer to the terms of use on [Link]

Conditions d'utilisation Ce document numérique peut être téléchargé gratuitement. Son statut juridique et ses conditions d'utilisation sont précisés dans sa notice détaillée. Pour de plus amples informations, voir [Link]

Condizioni di utilizzo Questo documento può essere scaricato gratuitamente. Il tipo di licenza e le condizioni di utilizzo sono indicate nella notizia bibliografica del singolo documento. Per ulteriori informazioni vedi anche [Link]

CAPVT IV.

EVOLVTIO AEQVATIONVM ORDINIS *iii* PRO LITTERIS Z ET Z.

§. 520.

Partes annexae harum aequationum ex aequationibus generalibus facile colliguntur sequentes:

$$\begin{aligned}
 \text{I. } 0 = & \dots + \mathfrak{B} \mathfrak{A} + Z \mathfrak{B} + 2 \mathfrak{U} \mathfrak{X} \mathfrak{C} + (\mathfrak{U} \mathfrak{X} + \mathfrak{U} \mathfrak{X}) \mathfrak{D} \\
 & + 2 \mathfrak{U} \mathfrak{X} \mathfrak{E} + \mathfrak{h} \mathfrak{U} (6 \lambda - 30 \lambda \mathfrak{D} + 90 \lambda \mathfrak{D}^2 - \frac{45}{4} \lambda \mathfrak{O}^2) \\
 & + \mathfrak{h} \mathfrak{U} (\frac{15}{2} \lambda \mathfrak{O} - 45 \lambda \mathfrak{D} \mathfrak{O}) \\
 & + \mathfrak{g} (-\frac{3}{2} \lambda + 6 \lambda \mathfrak{D} - 15 \lambda \mathfrak{D}^2 + \frac{15}{4} \lambda \mathfrak{O}^2) \\
 & + \frac{3}{4} \mathfrak{X} (2 \text{ cof. } t + 7 \text{ cof. } (2p - t) - \text{cof. } (2p + t)) \\
 & + \frac{3}{4} \mathfrak{X} (-7 \text{ sin. } (2p - t) + \text{sin. } (2p + t)).
 \end{aligned}$$

$$\begin{aligned}
 \text{II. } 0 = & \dots + \mathfrak{B} \mathfrak{A} + Z \mathfrak{B} + 2 \mathfrak{U} \mathfrak{X} \mathfrak{C} + (\mathfrak{U} \mathfrak{X} + \mathfrak{U} \mathfrak{X}) \mathfrak{D} \\
 & + 2 \mathfrak{U} \mathfrak{X} \mathfrak{E} + \mathfrak{h} \mathfrak{U} (\frac{15}{2} \lambda \mathfrak{O} - 45 \lambda \mathfrak{D} \mathfrak{O}) \\
 & + \mathfrak{h} \mathfrak{U} (-\frac{3}{2} \lambda + \frac{15}{2} \lambda \mathfrak{D} - \frac{45}{2} \lambda \mathfrak{D}^2 + \frac{45}{4} \lambda \mathfrak{O}^2) \\
 & + \mathfrak{g} (-\frac{3}{2} \lambda \mathfrak{O} + \frac{15}{2} \lambda \mathfrak{D} \mathfrak{O}) \\
 & + \frac{3}{4} \mathfrak{X} (-7 \text{ sin. } (2p - t) + \text{sin. } (2p + t)) \\
 & + \frac{3}{4} \mathfrak{X} (2 \text{ cof. } t - 7 \text{ cof. } (2p - t) + \text{cof. } (2p + t))
 \end{aligned}$$

vki

vbi $\frac{1}{2} = 2p\delta$, coefficientes vero hic occurrentes, iam in capite penultimo euoluimus.

§. 521.

Ante omnia igitur singula producta, quae hic occurrunt euolui conueniet, quae quidem nouem angulos in has tres classes distribuendos continebunt:

$$\begin{array}{ccc|ccc}
 \text{I.} & & \text{II.} & & \text{III.} & \\
 t & & t-2r & & t+2r & \\
 2p-t & & 2p-t+2r & & 2p-t-2r & \\
 2p+t & & 2p+t-2r & & 2p+t+2r &
 \end{array}$$

His notatis superiores formulas ordine petraetabimus:

I. $211\mathfrak{E}$ dat

$$\begin{aligned}
 &+0,00392.\text{cos. } t-0,01484.\text{cos. } (2p-t) \\
 &\quad +0,00160.\text{cos. } (2p+t) \\
 &-0,00206.\text{cos. } (t-2r)+0,00727.\text{cos. } (2p-t+2r) \\
 &\quad -0,00076.\text{cos. } (2p+t-2r) \\
 &-0,00164.\text{cos. } (t+2r)+0,00736.\text{cos. } (2p-t-2r) \\
 &\quad -0,00085.\text{cos. } (2p+t+2r)
 \end{aligned}$$

eius multiplicator

$$\begin{aligned}
 \text{I. } \int &+537,635924+15,4425816.\text{cos. } 2p \\
 \text{II. } \int &+10,9813978.\text{sin. } 2p.
 \end{aligned}$$

II.

II. (UX + UX) dat

$$\begin{aligned}
 & -0,04756. \sin. t + 0,00907. \sin. (2p-t) \\
 & \quad + 0,00102. \sin. (2p+t) \\
 & + 0,02295. \sin. (t-2r) - 0,00902. \sin. (2p-t+2r) \\
 & \quad - 0,00104. \sin. (2p+t-2r) \\
 & + 0,02443. \sin. (t+2r) - 0,00065. \sin. (2p-t-2r) \\
 & \quad + 0,00114. \sin. (2p+t+2r)
 \end{aligned}$$

eius multiplicator

$$\begin{aligned}
 \text{I. } & \int + 21,9627856. \sin. 2p \\
 \text{II. } & \int - 537,5635056 - 15,4452816. \cos. 2p
 \end{aligned}$$

III. 2 UX dat

$$\begin{aligned}
 & + 0,00081. \cos. t - 0,00409. \cos. (2p-t) \\
 & \quad + 0,00409. \cos. (2p+t) \\
 & - 0,04845. \cos. (t-2r) - 0,01074. \cos. (2p-t+2r) \\
 & \quad - 0,00785. \cos. (2p+t-2r) \\
 & + 0,04718. \cos. (t+2r) + 0,01716. \cos. (2p-t-2r) \\
 & \quad + 0,00143. \cos. (2p+t+2r)
 \end{aligned}$$

eius multiplicator

$$\begin{aligned}
 \text{I. } & \int - 268,7817528 - 7,721290. \cos. 2p \\
 \text{II. } & \int - 8,2360446. \sin. 2p.
 \end{aligned}$$

IV. h II dat

$$\begin{aligned}
 & - 0,00388. \cos. t + 0,01484. \cos. (2p-t) \\
 & \quad - 0,00161. \cos. (2p+t) \\
 & + 0,00225. \cos. (t-2r) - 0,00736. \cos. (2p-t+2r) \\
 & \quad + 0,00073. \cos. (2p+t-2r) \\
 & + 0,00162. \cos. (t+2r) - 0,00748. \cos. (2p-t-2r) \\
 & \quad + 0,00087. \cos. (2p+t+2r)
 \end{aligned}$$

A a a a

eius

eius multiplicator

I. $\int +1075,55190 + 38,606454 \cdot \text{cof. } 2p$

II. $\int +13,726741 \cdot \text{fin. } 2p.$

V. \oint U dat

$+0,09455 \cdot \text{fin. } t + 0,01831 \cdot \text{fin. } (2p-t)$

$-0,00061 \cdot \text{fin. } (2p+t)$

$-0,04684 \cdot \text{fin. } (t-2r) + 0,01097 \cdot \text{fin. } (2p-t+2r)$

$+0,00214 \cdot \text{fin. } (2p+t-2r)$

$-0,04757 \cdot \text{fin. } (t+2r) + 0,00731 \cdot \text{fin. } (2p-t-2r)$

$-0,00152 \cdot \text{fin. } (2p+t+2r)$

eius multiplicator

I. $\int +13,726741 \cdot \text{fin. } 2p$

II. $\int -268,809950 - 9,651614 \cdot \text{cof. } 2p.$

VI. \oint dat

$-0,00592 \cdot \text{cof. } t + 0,10356 \cdot \text{cof. } (2p-t)$

$-0,03969 \cdot \text{cof. } (2p+t)$

$+0,01991 \cdot \text{cof. } (t-2r) + 0,00678 \cdot \text{cof. } (2p-t+2r)$

$+0,03920 \cdot \text{cof. } (2p+t-2r)$

$-0,01590 \cdot \text{cof. } (t+2r) - 0,10898 \cdot \text{cof. } (2p-t-2r)$

$-0,00093 \cdot \text{cof. } (2p+t+2r)$

eius

eius multiplicator

$$\text{I. } \int -268,8518391 - 7,7212908. \text{ cof. } 2p$$

$$\text{II. } \int -2,7453482. \text{ fin. } 2p.$$

Postremae partes aequationis primae dant:

$$-0,28373. \text{ cof. } t - 1,29893. \text{ cof. } (2p - t)$$

$$+0,20210. \text{ cof. } (2p + t)$$

$$+0,06313. \text{ cof. } (t - 2r) + 0,00256. \text{ cof. } (2p - t + 2r)$$

$$-0,19447. \text{ cof. } (2p + t - 2r)$$

$$+0,20288. \text{ cof. } (t + 2r) + 1,28673. \text{ cof. } (2p - t - 2r)$$

$$-0,00002. \text{ cof. } (2p + t + 2r)$$

Postremae partes secundae aequationis dant

$$+0,12218. \text{ fin. } t + 1,29739. \text{ fin. } (2p - t)$$

$$-0,20373. \text{ fin. } (2p + t)$$

$$+0,06307. \text{ fin. } (t - 2r) - 0,00217. \text{ fin. } (2p - t + 2r)$$

$$+0,18515. \text{ fin. } (2p + t - 2r)$$

$$-0,20028. \text{ fin. } (t + 2r) - 1,29605. \text{ fin. } (2p - t - 2r)$$

$$+0,00002. \text{ fin. } (2p + t + 2r).$$

Hae expressiones singulae manifeste in tres portiones distinguuntur, quas seorsim tractari conuenit.

A a a a 2

Euolu-

Euolutio I. terminorum angulum t simpliciter continentium.

§. 522.

Ex partibus cognitis primae aequationis eliciatur \mathfrak{M} hoc modo :

	t	$2p - t$	$2p + t$
$2 \text{ U } \mathfrak{X} (+ 537, 63) -$	+ 2,10753	- 7,97852	+ 0,86022
	- 0,11459		
$2 \text{ U } \mathfrak{X} (+ 15,442. \text{ cof. } 2p)$	+ 0,01235	+ 0,03027	+ 0,03027
	+ 2,00529	- 7,94825	+ 0,89049
$(\text{U } \mathfrak{X} + \text{U } \mathfrak{X})(+ 21. \text{ sin. } 2p)$	+ 0,09960	- 0,52227	+ 0,52227
	+ 0,01120		
	+ 0,11080		
	+ 2,11609	- 8,47052	+ 1,41276
$2 \text{ U } \mathfrak{X} (- 268, 78) -$	- 0,21772	+ 1,09932	- 1,09932
$2 \text{ U } \mathfrak{X} (- 7, 721. \text{ cof. } 2p)$	- 0,00000	- 0,00313	- 0,00313
		+ 1,09619	- 1,10245
	+ 1,89837	- 7,37433	+ 0,31031
$\mathfrak{b} \text{ U} (+ 1075, 55) -$	- 4,17314	+ 15,96119	- 1,73164
	+ 0,28646	- 0,07489	- 0,07489
$\mathfrak{b} \text{ U} (+ 38, 606. \text{ cof. } 2p)$	- 0,03108		
	- 3,91776	+ 15,88630	- 1,80653
	- 2,01939	+ 8,51197	- 1,49622
$\mathfrak{b} \text{ U} (+ 13, 726. \text{ sin. } 2p)$	- 0,12567	+ 0,64893	- 0,64893
	- 0,00419		
	- 0,12986		
	- 2,14925	+ 9,16090	- 2,14515
$\mathfrak{g} (- 268, 85) - -$	+ 1,59160	- 27,84229	+ 10,67027
$\mathfrak{g} (- 7, 721. \text{ cof. } 2p)$	- 0,40008	+ 0,02287	+ 0,02287
	- 0,15334		
	+ 1,03818	- 27,81942	+ 10,69314
	- 1,11107	- 18,65852	+ 8,54799
Pars post.	- 0,28373	- 1,29893	+ 0,20210
$\mathfrak{M} =$	- 1,39480	- 19,95745	+ 8,75009

§. 523.

§. 523.

Eodem modo ex secunda aequatione eliciamus M:

	t	$2p - t$	$2p + t$
$2U\mathfrak{X}(+10,981. \text{fin. } 2p)$	- 0,08148	+ 0,02152	+ 0,02152
	- 0,00879		
	- 0,09027		
$(UX+U\mathfrak{X})(-537,56.)$	+ 25,56651	- 4,87570	- 0,54831
	+ 0,07003	- 0,36723	+ 0,36723
$(UX+U\mathfrak{X})(-15,44 \text{ cof. } 2p)$	- 0,00788		
	+ 25,62866	- 5,24293	- 0,18108
	+ 25,53839	- 5,22141	- 0,15956
$2UX(-8,236. \text{fin. } 2p)$	+ 0,03368	- 0,00334	- 0,00334
	+ 25,57207	- 5,22475	- 0,16290
$\mathfrak{U}(+13,72. \text{fin. } 2p)$	+ 0,10185	- 0,02603	- 0,02663
	+ 0,01105		
	+ 0,11290		
	+ 25,68497	- 5,25138	- 0,18953
$\mathfrak{U}(-268,809.) -$	- 25,41597	+ 4,92191	+ 0,16397
	- 0,08836	+ 0,45628	- 0,45628
$\mathfrak{U}(-9,65. \text{cof. } 2p)$	+ 0,00294		
	- 25,50139	+ 5,37819	- 0,29231
	+ 0,18358	+ 0,12681	- 0,48184
$\mathfrak{U}(-2,745. \text{fin. } 2p)$	- 0,14215	+ 0,00812	+ 0,00812
	- 0,05448		
	- 0,19663		
	- 0,01305	+ 0,13493	- 0,47372
Pars poster.	+ 0,12218	+ 1,29739	- 0,20373
M =	+ 0,10913	+ 1,43232	- 0,67745

Aaaa 3

§. 524.

§. 524.

Quoniam elementa numerica iam supra Capite VII. sunt tradita, hinc statim quaeramus litteras \mathfrak{N} et \mathfrak{N} :

	t	$2p-t$	$2p+t$
L. M	+ 9,0379442	+ 0,1560400	- 9,8308772
$L. \frac{2(m+1)}{\mu}$	+ 1,4271258	+ 0,0516847	+ 0,0165527
$L. \frac{2(m+1)M}{\mu}$	+ 0,4650700	+ 0,2077247	- 9,8474299
$\frac{2(m+1)M}{\mu}$	+ 2,9179	+ 1,6133	- 0,7037
- \mathfrak{M}	+ 1,3948	+ 19,9574	- 8,7501
Numer.	+ 4,3127	+ 21,5707	- 9,4538
L. Num.	+ 0,6347492	+ 1,3338642	- 0,9756064
L. den.	+ 2,2460771	- 2,5722026	- 2,6859274
Log. \mathfrak{N}	+ 8,3886721	- 8,7616616	+ 8,2896790
$L. \frac{2(m+1)}{\mu}$	+ 1,4271258	+ 0,0516847	+ 0,0165527
L. P. II.	+ 9,8157979	- 8,8133463	+ 8,3062317
Log. M	+ 9,0379442	+ 0,1560400	- 9,8308772
Log. μ^2		+ 2,7408822	+ 2,8211442
L. P. I.	+ 9,0379442	+ 7,4151578	- 7,0097330
P. I.	+ 0,1091	+ 0,0026	- 0,0010
- P. II.	- 0,6543	+ 0,0651	- 0,0202
N	- 0,5452	+ 0,0677	- 0,0212
\mathfrak{N}	+ 0,0244	- 0,0577	+ 0,0195

§. 525.

§. 525.

Pro partibus autem incognitis statuamus

$$Z = \beta \cdot \text{cof. } t + \gamma \cdot \text{cof. } (2p-t) + \delta \cdot \text{cof. } (2p+t)$$

$$Z = b \cdot \text{fin. } t + c \cdot \text{fin. } (2p-t) + d \cdot \text{fin. } (2p+t)$$

vnde quaeramus litteras M' et M' :Pro M' .

$$\begin{array}{l} Z(-9,221 \cdot \text{cof. } 2p) = \\ Z(+0,02644) = \\ Z(-3,990 \cdot \text{fin. } 2p) = \end{array} \begin{array}{l} \text{cof. } t \\ -4,61064 \cdot (\gamma + \delta) \\ +0,02644 \cdot \beta \\ -1,99534 \cdot (c+d) \end{array} \begin{array}{l} \text{cof. } (2p-t) \\ -4,61064 \cdot \beta \\ +0,02644 \cdot \gamma \\ -1,99534 \cdot b \end{array} \begin{array}{l} \text{cof. } (2p+t) \\ -4,61064 \cdot \beta \\ +0,02644 \cdot \delta \\ -1,99534 \cdot b \end{array}$$

Pro M' .

$$\begin{array}{l} Z(-3,990 \cdot \text{cof. } 2p) = \\ Z(+5,360 \cdot \text{cof. } 2p) = \\ Z(-0,0272) = \end{array} \begin{array}{l} \text{fin. } t \\ -1,995 \cdot (\gamma - \delta) \\ -2,680 \cdot (c-d) \\ -0,0272 \cdot b \end{array} \begin{array}{l} \text{fin. } (2p-t) \\ -1,995 \cdot \beta \\ -2,680 \cdot b \\ -0,0272 \cdot c \end{array} \begin{array}{l} \text{fin. } (2p+t) \\ -1,995 \cdot \beta \\ +2,680 \cdot b \\ -0,0272 \cdot d \end{array}$$

§. 526.

§. 526.

Euoluamus igitur vt hactenus secundum angulum $(2p - i)$:

	β	b	γ	c
L. M'	- 0,3000187	- 0,4281870		- 8,43515
$L. \frac{2(m+1)}{\mu}$	+ 0,0516847	+ 0,0516847		+ 0,05168
$L. \frac{2(m+1)M}{\mu}$	- 0,3517034	- 0,4798717		- 8,48683
$\frac{2(m+1)M'}{\mu}$	- 2,2475	- 3,0191		- 0,0307
- M'	+ 4,6106	+ 1,9953	- 0,0264	
Numer.	+ 2,3631	- 1,0238	- 0,0264	- 0,0307
L. Num.	+ 0,3734821	- 0,0102151	- 8,42160	- 8,48683
L. Den.	- 2,5722026	- 2,5722026	- 2,57220	- 2,57220
Log. N'	- 7,8012795	+ 7,4380125	+ 5,84940	+ 5,91463
$L. \frac{2(m+1)}{\mu}$	+ 0,0516847	+ 0,0516847	+ 0,05168	+ 0,05168
L. P. II.	- 7,8529642	+ 7,4896972	+ 5,90108	+ 5,96631
Log. M'	- 0,3000187	- 0,4281870		- 8,43515
Log. μ^2	+ 2,7408822	+ 2,7408822		+ 2,74088
L. P. I.	- 7,5591365	- 7,6873048		- 5,69427
P. I.	- 0,0036	- 0,0049		- 0,00005
- P. II.	+ 0,0071	- 0,0031	- 0,00008	- 0,00009
N'	+ 0,0035	- 0,0080	- 0,00008	- 0,00014
N'	- 0,0063	+ 0,0027	+ 0,00007	+ 0,00008

$$\text{hinc } \gamma = -0,0577 - 0,0063 \cdot \beta + 0,0027 \cdot b$$

$$c = +0,0677 + 0,0035 \cdot \beta - 0,0080 \cdot b$$

impune enim bina postrema membra omittere licet.

§. 527.

§. 527.

In sequente ergo calculo statim, multo magis
binas postremas columnas omittere poterimus;

Pro angulo ($2p + t$)

	β	b
L. M'	- 0,3000187	+ 0,4281870
L. $\frac{2(m+1)}{\mu}$	+ 0,0165527	+ 0,0165527
L. $\frac{2(m+1)M'}{\mu}$	- 0,3165714	+ 0,4447397
$\frac{2(m+1)M'}{\mu}$	- 2,0729	+ 2,7844
- M'	+ 4,6106	+ 1,9953
Numer.	+ 2,5377	+ 4,7797
L. Num.	+ 0,4044403	+ 0,6794097
L. Den.	- 2,6859274	- 2,6859274
L. \mathcal{N}'	- 7,7185129	- 7,9934823
L. $\frac{2(m+1)}{\mu}$	+ 0,0165527	+ 0,0165527
L. P. II.	- 7,7350656	- 8,0100350
Log. M'	- 0,3000187	+ 0,4281870
Log. μ^2	+ 2,8211442	+ 2,8211442
L. P. I.	- 7,4788745	+ 7,6070428
Pars I.	- 0,0030	+ 0,0040
- P. II.	+ 0,0054	+ 0,0102
N'	+ 0,0024	+ 0,0142
\mathcal{N}'	- 0,0052	- 0,0099

B b b b

hinc

hinc

$$\delta = +0,0195 - 0,0052. \beta - 0,0099. b$$

$$d = -0,0212 + 0,0024. \beta + 0,0142. b$$

§. 528.

Quum iam hinc sit

$$\gamma + \delta = -0,0382 - 0,0115. \beta - 0,0072. b;$$

$$\gamma - \delta = -0,0772 - 0,0011. \beta + 0,0126. b;$$

$$c + d = +0,0465 + 0,0059. \beta + 0,0062. b;$$

$$c - d = +0,0889 + 0,0011. \beta - 0,0222. b;$$

pro angulo primo ϵ reperimus

$$M' = +0,0833 + 0,0412. \beta + 0,0211. b$$

$$M'' = -0,0842 - 0,0007. \beta + 0,0344. b$$

§. 529.

§. 529.

His igitur quaeramus respondentes \mathfrak{N} et \mathfrak{N}' :Pro angulo t .

	i .	β	δ
Log. M'	- 8,9253121	- 6,8450980	+ 8,5365584
$L. \frac{2^{(m+1)}}{\mu}$	+ 1,4271258	+ 1,4271258	+ 1,4271258
$L. \frac{2^{(m+1)M'}}{\mu}$	- 0,3524379	- 8,2722238	+ 9,9636842
$\frac{2^{(m+1)M'}}{\mu}$	- 2,2513	- 0,0187	+ 0,9197
- \mathfrak{M}'	- 0,0833	- 0,0412	- 0,0211
Numer.	- 2,3346	- 0,0599	+ 0,8986
L. Num.	- 0,3682125	- 8,7774268	+ 9,9535664
L. Den.	+ 2,2460771	+ 2,2460771	+ 2,2460771
L. \mathfrak{N}'	- 8,1221354	- 6,5313497	+ 7,7074893
$L. \frac{2^{(m+1)}}{\mu}$	+ 1,4271258	+ 1,4271258	+ 1,4271258
L. P. II	- 9,5492612	- 7,9584755	+ 9,1346151
L. P. I.	- 8,92531	- 6,84509	+ 8,53655
P. I.	- 0,0842	- 0,0007	+ 0,0344
- P. II.	+ 0,3542	+ 0,0091	- 0,1363
\mathfrak{N}'	+ 0,2700	+ 0,0084	- 0,1019
\mathfrak{N}	- 0,0133	- 0,0003	+ 0,0051

Hinc

$$\beta = +0,0111 - 0,0003. \beta + 0,0051. b$$

$$b = -0,2752 + 0,0084. \beta - 0,1019. b$$

ex priori fit

$$\beta = +0,0111 + 0,0051. b,$$

qui valor in altera substitutus praebet

$$b = -0,2751 - 0,1019. b,$$

vnde colligitur

$$b = -0,2496; \text{ ideoque } \beta = +0,0098;$$

$$\gamma = -0,0584; c = +0,0697;$$

$$\delta = +0,0220; d = -0,0247;$$

ita vt haec euolutio prima nobis exhibeat:

$$S = +0,0098. \cos. t - 0,0584. \cos. (2p - t)$$

$$+ 0,0220. \cos. (2p + t)$$

$$Z = -0,2496. \sin. t + 0,0697. \sin. (2p - t)$$

$$- 0,0247. \sin. (2p + t).$$

II. Evolutio terminorum angulum ($t - 2r$) inuoluentium.

§. 530.

Hinc igitur superiorum formularum partes secundas sumimus, ac primo quidem ex priori aequatione colligamus litteram \mathfrak{M} :

	$t - 2r$	$2p - t + 2r$	$2p + t - 2r$
$2 \mathfrak{U} \mathfrak{X} (537, 63) -$	- 1,10753	+ 3,90861	- 0,40860
	+ 0,05613	- 0,01591	- 0,01591
$2 \mathfrak{U} \mathfrak{X} (+ 15,442. \text{cof. } 2p)$	- 0,00587		
	- 1,05727	+ 3,89270	- 0,42451
$(\mathfrak{U} \mathfrak{X} + \mathfrak{U} \mathfrak{X})(2r. \text{fin. } 2p)$	- 0,09905	+ 0,25202	- 0,25202
	- 0,01142		
	- 0,11047		
	- 1,16774	+ 4,14472	- 0,67652
$2 \mathfrak{U} \mathfrak{X} (- 268, 78) -$	+ 13,02247	+ 2,88672	+ 2,10994
	+ 0,04149	+ 0,18718	+ 0,18718
$2 \mathfrak{U} \mathfrak{X} (- 7, 72r. \text{cof. } 2p)$	+ 0,03033		
	+ 13,09429	+ 3,07390	+ 2,29712
	+ 11,92655	+ 7,21862	+ 1,62060
$\mathfrak{U} \mathfrak{U} (+ 1075, 55) -$	+ 2,41999	- 7,91606	+ 0,78515
	- 0,14207	+ 0,04343	+ 0,04343
$\mathfrak{U} \mathfrak{U} (+ 38,606. \text{cof. } 2p)$	+ 0,01409		
	+ 2,29201	- 7,87263	+ 0,82858
	+ 14,21856	- 0,65401	+ 2,44918
$\mathfrak{U} \mathfrak{U} (+ 13,726. \text{fin. } 2p)$	+ 0,07529	- 0,32148	+ 0,32148
	+ 0,01469		
	+ 0,08998		
	+ 14,30854	- 0,97549	+ 2,77066
$\mathfrak{U} (- 268, 85) -$	- 5,35284	- 1,82282	- 10,53899
	- 0,02619	- 0,07692	- 0,07692
$\mathfrak{U} (- 7, 72. \text{cof. } 2p)$	- 0,15144		
	- 5,53047	- 1,89974	- 10,61591
	+ 8,77807	- 2,87523	- 7,84525
Part. poster.	+ 0,06313	+ 0,00256	- 0,19447
$\mathfrak{M} =$	+ 8,84120	- 2,87267	- 8,03972

B b b b 3

§. 531.

Simili modo ex secunda aequatione elicimus M:

	$t - 2r$	$2p - t + 2r$	$2p + t - 2r$
$2UX (+10,98. \text{fin. } 2p)$	+ 0,03991	- 0,01131	- 0,01131
	+ 0,00417		
	+ 0,04408		
$(UX + U\mathfrak{E})(-537,56)$	- 12,33709	+ 4,84882	+ 0,55906
	- 0,06964	+ 0,17721	- 0,17721
$(UX + U\mathfrak{E})(-15,44. \text{cf. } 2p)$	+ 0,00803		
	- 12,39870	+ 5,02603	+ 0,38185
	- 12,35462	+ 5,01472	+ 0,37054
$2UX (-8,236. \text{fin. } 2p)$	+ 0,04423	+ 0,19952	+ 0,19952
	- 0,03233		
	+ 0,01190		
	- 12,34272	+ 5,21424	+ 0,57006
$\mathfrak{H}U (+13,726. \text{fin. } 2p)$	- 0,05051	+ 0,01544	+ 0,01544
	- 0,00501		
	- 0,05552		
	- 12,39824	+ 5,22968	+ 0,58550
$\mathfrak{H}U (-268,809) -$	+ 12,59106	- 2,94884	- 0,57525
	+ 0,05294	- 0,22604	+ 0,22604
$\mathfrak{H}U (-9,651. \text{cf. } 2p)$	- 0,01032		
	+ 12,63368	- 3,17488	- 0,34921
	+ 0,23544	+ 2,05480	+ 0,23629
$\mathfrak{H}(-2,745. \text{fin. } 2p)$	- 0,01044	- 0,02733	- 0,02733
	+ 0,05381		
	+ 0,04337		
	+ 0,27881	+ 2,02747	+ 0,20896
Part. poster.	+ 0,06307	- 0,00217	+ 0,18515
M =	+ 0,34188	+ 2,02530	+ 0,39411

§. 532.

Euoluantur iam pro his angulis elementa numerica :

$\omega =$	$t - 2r$	$2p - t + 2r$	$2p + t - 2r$
$\mu =$	$1 - 2l$	$2m - 1 + 2l$	$2m + 1 - 2l$
feu $\mu =$	-25,84526	+50,58310	-1,10742
Log. $\mu =$	-1,4123792	+1,7040055	-0,0443123
Log. $2(m+1) =$	+1,4271258	+1,4271258	+1,4271258
Log. $\frac{2(m+1)}{\mu} =$	-0,0147466	+9,7231203	-1,3828135
Log. $\mu^2 =$	-2,8247584	+3,4080110	+0,0886246
$\lambda - 2 =$	177,22893	177,22893	177,22893
$-\mu^2 =$	-667,97275	-2558,65059	-1,22638
Denom. =	-490,74382	-2381,42166	-176,00255

§. 533.

Horum elementorum ope determinemus litteras
 \mathfrak{N} et N pro binis angulis posterioribus:

L. M	+ 0,3064894	+ 9,5956175
$L. \frac{2(m+1)}{\mu}$	+ 9,7231203	- 1,3828135
$L. \frac{2(m+1)M}{\mu}$	+ 0,0296097	- 0,9784310
$\frac{2(m+1)M}{\mu}$	+ 1,07056	- 9,51549
- \mathfrak{M}	+ 2,87267	+ 8,03972
Numer.	+ 3,94323	- 1,47577
L. Num.	+ 0,5958521	- 0,1690192
L. Den.	- 3,3768361	+ 2,2455189
L. \mathfrak{N}	- 7,2190160	- 7,9235003
$L. \frac{2(m+1)}{\mu}$	+ 9,7231203	- 1,3828135
L. P. II.	- 6,9421363	+ 9,3063138
L. M	+ 0,3064894	+ 9,5956175
L. μ^2	+ 3,4080110	+ 0,0886246
L. P. I.	+ 6,8984784	+ 9,5069929
P. I.	+ 0,0008	+ 0,3214
- P. II.	+ 0,0009	- 0,2025
N	+ 0,0017	+ 0,1189
at \mathfrak{N}	- 0,0017	- 0,0084

§. 534.

§. 534.

Pro partibus incognitis ponamus vt haecenus:

$$\mathfrak{S} = \beta. \text{ cof. } (t - 2r) + \gamma. \text{ cof. } (2p - t + 2r) \\ + \delta. \text{ cof. } (2p + t - 2r)$$

$$Z = b. \text{ fin. } (t - 2r) + c. \text{ fin. } (2p - t + 2r) \\ + d. \text{ fin. } (2p + t - 2r)$$

vnde quaeramus litteras \mathfrak{M} et \mathfrak{M}' :

Pro \mathfrak{M} :

$$\begin{array}{l} \mathfrak{S}(-9,221. \text{ cof. } 2p) \\ \mathfrak{S}(+0,0264) \\ Z(-3,990. \text{ fin. } 2p) \end{array} \left| \begin{array}{l} \text{cof. } (t - 2r) \\ -4,6106. (\gamma + \delta) \\ +0,0264. \beta \\ -1,995. (c + d) \end{array} \right| \left| \begin{array}{l} \text{cf. } (2p - t + 2r) \\ -4,6106. \beta \\ +0,0264. \gamma \\ -1,995. b \end{array} \right| \left| \begin{array}{l} \text{cof. } (2p + t - 2r) \\ -4,6106. \delta \\ +0,0264. d \\ -1,995. b \end{array} \right|$$

Pro \mathfrak{M}' :

$$\begin{array}{l} \mathfrak{S}(-3,990. \text{ fin. } 2p) \\ Z(+5,360. \text{ cof. } 2p) \\ Z(-0,0272) \end{array} \left| \begin{array}{l} \text{fin. } (t - 2r) \\ -1,995. (\gamma - \delta) \\ -2,6803. (c - d) \\ -0,0272. b \end{array} \right| \left| \begin{array}{l} \text{fi. } (2p - t + 2r) \\ -1,995. \beta \\ -2,6803. b \\ -0,0272. c \end{array} \right| \left| \begin{array}{l} \text{fi. } (2p + t - 2r) \\ -1,995. \delta \\ +2,6803. d \\ -0,0272. d \end{array} \right|$$

C c c c

§. 535.

§. 535.

Hinc calculum litterarum \mathfrak{N}' et \mathfrak{N} incipiamus
ab angulo postremo

	β	b	δ	d
Log. M'	- 0,3000187	+ 0,4281870		- 8,4351545
$L. \frac{2(m+1)}{\mu}$	- 1,3828135	- 1,3828135		- 1,3828135
$L. \frac{2(m+1)M'}{\mu}$	+ 1,6828322	- 1,8110005		+ 9,8179680
$\frac{2(m+1)M'}{\mu}$	+ 48,17616	- 64,71434		+ 0,65761
- \mathfrak{M}'	+ 4,61064	+ 1,99534	- 0,02644	
Num.	+ 52,78680	- 62,71900	- 0,02644	+ 0,65761
L. Num.	+ 1,7225253	- 1,7973991	- 8,4216039	+ 9,8179680
L. Den.	+ 2,2455189	+ 2,2455189	+ 2,2455189	+ 2,2455189
Log. \mathfrak{N}'	+ 9,4770064	- 9,5518802	- 6,1760850	+ 7,5724491
$L. \frac{2(m+1)}{\mu}$	- 1,3828135	- 1,3828135	- 1,3828135	- 1,3828135
L. P. II.	- 0,8598199	+ 0,9346937	+ 7,5588985	- 8,9552626
Log. M'	- 0,3000187	+ 0,4281870		- 8,4351545
Log. μ^2	+ 0,0886246	+ 0,0886246		+ 0,0886246
Log. P. I.	- 0,2113941	+ 0,3395624		- 8,3465299
P. I.	- 1,62702	+ 2,18556		- 0,02221
P. II.	+ 7,24135	- 8,60387	- 0,00362	+ 0,09021
\mathfrak{N}'	+ 5,6143	- 6,4183	- 0,0036	+ 0,0680
\mathfrak{N}	+ 0,2999	- 0,3564	- 0,0002	+ 0,0038

hinc

$$\delta = -0,0084 + 0,2999 \beta - 0,3564 \cdot b - 0,0002 \delta + 0,0038 \cdot d$$

$$d = +0,1189 + 5,6143 \cdot \beta - 6,4183 \cdot b - 0,0036 \cdot \delta + 0,0680 \cdot d$$

vnde

vnde concludimus

$$\delta = -0,0079 + 0,3226. \beta - 0,3825. b$$

$$d = +0,1279 + 6,0225. \beta - 6,8852. b$$

§. 536.

Eodem modo tractemus secundum angulum $2p - t + 2r$, vbi facile patet binas postremas columnas γ et c praetermitti posse:

	β	b
L. M'	- 0,3000187	- 0,4281870
L. $\frac{2(m+1)}{\mu}$	+ 9,7231203	+ 9,7231203
L. $\frac{2(m+1)M'}{\mu}$	- 0,0231390	- 0,1513073
$\frac{\mu}{2(m+1)M'}$	- 1,0547	- 1,4168
- M'	+ 4,6106	+ 1,9953
Numer.	+ 3,5559	+ 0,5785
L. Num.	+ 0,5509495	+ 9,7623034
L. Den.	- 3,3768361	- 3,3768361
Log. N'	- 7,1741134	- 6,3854673
L. $\frac{2(m+1)}{\mu}$	+ 9,7231203	+ 9,7231203
L. P II.	- 6,8972337	- 6,1085876
Log. M'	- 0,3000187	- 0,4281870
Log. μ^2	+ 3,4080110	+ 3,4080110
L. P. I.	- 6,8920077	- 7,0201760
P. I.	- 0,0008	- 0,0010
- P. II.	+ 0,0008	+ 0,0001
N'	- 0,0000	- 0,0009
N'	- 0,0015	- 0,0002

Cccc 2

hinc

hinc

$$\gamma = -0,0017 - 0,0015. \beta - 0,0002. b$$

$$\epsilon = +0,0017 + 0,0000. \beta - 0,0009. b$$

§. 537.

Quum igitur nunc habeamus:

$$\gamma + \delta = -0,0096 + 0,3211. \beta - 0,3827. b$$

$$\gamma - \delta = +0,0062 - 0,3241. \beta + 0,3823. b$$

$$c + d = +0,1296 + 6,0225. \beta - 6,8861. b$$

$$c - d = -0,1262 - 6,0225. \beta + 6,8843. b$$

• reperiemus pro angulo primo $t - 2r$

$$M + M' = +8,62686 - 13,47102. \beta$$

$$+ 15,50467. b$$

et

$$M + M' = +0,66777 + 16,78893. \beta$$

$$- 19,24220. b.$$

§. 538.

§. 538.

His ergo valoribus sequens calculus superstruat-
tur pro angulo $t - 2r$.

	α	β	b
L. M	+ 9,8246334	+ 1,2240233	- 1,2842547
$L. \frac{2(m+1)}{\mu}$	- 0,0147466	- 0,0147466	- 0,0147466
$L. \frac{2(m+1)M}{\mu}$	- 9,8393800	- 1,2387699	+ 1,2990013
$\frac{2(m+1)M}{\mu}$	- 0,69085	- 17,32886	+ 19,90679
- M	- 8,62686	+ 13,47102	- 15,50467
Num.	- 9,31771	- 3,85784	+ 4,40212
L. Num.	- 0,9693092	- 0,5863443	+ 0,6436619
L. Den.	- 2,6908549	- 2,6908549	- 2,6908549
L. N	+ 8,2784543	+ 7,8954894	- 7,9528070
$L. \frac{2(m+1)}{\mu}$	- 0,0147466	- 0,0147466	- 0,0147466
L. P. II.	- 8,2932009	- 7,9102360	+ 7,9675536
L. M	+ 9,8246334	+ 1,2240233	- 1,2842547
L. μ^2	+ 2,8247584	+ 2,8247584	+ 2,8247584
L. P. I.	+ 6,9998750	+ 8,3992649	- 8,4594963
P. I.	+ 0,0010	+ 0,0251	- 0,0288
- P. II.	+ 0,0196	+ 0,0082	- 0,0073
N	+ 0,0206	+ 0,0333	- 0,0381
N	+ 0,0190	+ 0,0079	- 0,0090

hinc

$$\beta = +0,0190 + 0,0079. \beta - 0,0090. b \text{ et}$$

$$b = +0,0206 + 0,0333. \beta - 0,0381. b$$

ex posteriori deducimus

$$b = +0,0198 + 0,0321. \beta,$$

qui valor in prima substitutus praebet

$$\beta = +0,0188 + 0,0076. \beta,$$

vnde

$$\beta = +0,0189 \text{ et } b = +0,0204,$$

vnde sequentes deducuntur valores:

$$\gamma = -0,0017; c = +0,0017;$$

$$\delta = -0,0096; d = +0,1016.$$

ita vt haec secunda euolutio nobis suppeditet:

$$\begin{aligned} \mathfrak{B} = & +0,0189. \text{cof.}(t-2r) - 0,0017. \text{cof.}(2p-t+2r) \\ & - 0,0096. \text{cof.}(2p+t-2r) \end{aligned}$$

$$\begin{aligned} \mathfrak{Z} = & +0,0204. \text{fin.}(t-2r) + 0,0017. \text{fin.}(2p-t+2r) \\ & + 0,1016. \text{fin.}(2p+t-2r). \end{aligned}$$

III. Euolutio terminorum angulum $t + 2r$ inuoluentium.

§. 539.

Calculus pro litteris \mathfrak{M} ita se habet :

	$t + 2r$	$2p - t - 2r$	$2p + t + 2r$
$2 \mathfrak{U} \mathfrak{X} (+ 537, 63) -$	- 0,88172	+ 3,95700	- 0,45699
	+ 0,05683	- 0,01266	- 0,01266
$2 \mathfrak{U} \mathfrak{X} (+ 15,442. \text{cof. } 2p)$	- 0,00656		
	- 0,83145	+ 3,94434	- 0,46965
$(\mathfrak{U} \mathfrak{X} + \mathfrak{U} \mathfrak{X}) (+ 21. \text{fin. } 2p)$	- 0,00714	+ 0,26828	- 0,26828
	+ 0,01252		
	+ 0,00538		
	- 0,82607	+ 4,21262	- 0,73793
$2 \mathfrak{U} \mathfrak{X} (- 268, 78) -$	- 12,68110	- 4,61230	- 0,38436
	- 0,06629	- 0,18227	- 0,18227
$2 \mathfrak{U} \mathfrak{X} (- 7, 721. \text{cof. } 2p)$	- 0,00553		
	- 12,75292	- 4,79457	- 0,56663
	- 13,57899	- 0,58195	- 1,30456
$\mathfrak{H} \mathfrak{U} (+ 1075, 55) -$	+ 1,74239	- 8,04513	+ 0,93573
	- 0,14439	+ 0,03127	+ 0,03127
$\mathfrak{H} \mathfrak{U} (+ 38, 606. \text{cof. } 2p)$	+ 0,01679		
	+ 1,61479	- 8,01386	+ 0,96700
	- 11,96420	- 8,59581	- 0,33756
$\mathfrak{H} \mathfrak{U} (+ 13, 726. \text{fin. } 2p)$	+ 0,05017	- 0,32649	+ 0,32649
	- 0,01043		
	+ 0,03974		
	- 11,92446	- 8,62230	- 0,01107
$\mathfrak{G} (- 268, 85) - -$	+ 4,54359	+ 29,29945	+ 0,25003
$\mathfrak{G} (- 7, 721. \text{cof. } 2p)$	+ 0,42102	+ 0,06529	+ 0,06529
	+ 0,00359		
	+ 4,96820	+ 29,36474	+ 0,31532
	- 6,95626	+ 20,74244	+ 0,30425
Pars post.	+ 0,20288	+ 1,28673	- 0,00002
$\mathfrak{M} =$	- 6,75338	+ 22,02917	+ 0,30423

§. 540.

§. 540.

Simili modo sequens calculus se habebit pro M :

	$t + 2r$	$2p - t - 2r$	$2p + t + 2r$
$211\mathfrak{X}(+10,981. \text{fin. } 2p)$	+ 0,04041	- 0,00900	- 0,00900
	+ 0,00467		
	+ 0,04508		
$(11X+U\mathfrak{X})(-537,56.)$	- 13,13268	+ 0,34942	- 0,61282
	- 0,00502	+ 0,18863	- 0,18863
$(11X+U\mathfrak{X})(-15,44 \text{ cof. } 2p)$	- 0,00880		
	- 13,14650	+ 0,53805	- 0,80145
	- 13,10142	+ 0,52905	- 0,81045
$2UX(-8,236. \text{fin. } 2p)$	- 0,07066	- 0,19429	- 0,19429
	+ 0,00589		
	- 0,06477		
	- 13,16619	+ 0,33476	- 1,00474
$\mathfrak{H}(+13,72. \text{fin. } 2p)$	- 0,05134	+ 0,01112	+ 0,01112
	- 0,00597		
	- 0,05731		
	- 13,22350	+ 0,34588	- 0,99362
$\mathfrak{U}(-268,809.) -$	+ 12,78729	- 1,96500	+ 0,40859
	+ 0,03528	- 0,22957	+ 0,22957
$\mathfrak{U}(-9,65. \text{cof. } 2p)$	+ 0,00734		
	+ 12,82991	- 2,19457	+ 0,53816
	- 0,39359	- 1,84869	- 0,45546
$\mathfrak{G}(-2,745. \text{fin. } 2p)$	+ 0,14959	+ 0,02320	+ 0,02320
	- 0,00128		
	+ 0,14831		
	- 0,24528	- 1,82549	- 0,43226
Pars poster.	- 0,20028	- 1,29605	+ 0,00002
M =	- 0,44556	- 3,12154	- 0,43224

§. 541.

§. 541.

Elementa numerica ex praecedentibus facile formantur :

$\omega =$	$t + 2r$	$2p - t - 2r$	$2p + t + 2r$
$\mu =$	$1 + 2l$	$2m - 1 - 2l$	$2m + 1 + 2l$
feu $\mu =$	+ 27,84526	- 3,10742	+ 52,58310
$L. 2(m+1) =$	+ 1,4271258	+ 1,4271258	+ 1,4271258
$\text{Log. } \mu =$	+ 1,4447512	- 0,4924000	+ 1,7208462
$L. \frac{2(m+1)}{\mu} =$	+ 9,9823746	- 0,9347258	+ 9,7062796
$\text{Log. } \mu^2 =$	+ 2,8895024	+ 0,9848000	+ 3,4416924
$\lambda - 2 =$	+ 177,22893	+ 177,22893	+ 177,22893
$-\mu^2 =$	- 775,35830	- 9,65606	- 2764,98300
$\text{Log. Den.} =$	- 598,12937	+ 167,57287	- 2587,75407

§. 542.

Hic iterum prima columna omiffa, calculum pro binis fequentibus faciamus:

	$2p - t - 2r$	$2p + t + 2r$
Log. M	-0,4943689	-9,6357250
Log. $\frac{2(m+1)}{\mu}$	-0,9347258	+9,7062796
Log. $\frac{2(m+1)M}{\mu}$	+1,4290947	-9,3420046
$\frac{2(m+1)M}{\mu}$	+26,85930	-0,21979
- M	-22,02917	-0,30423
Numerat.	+4,83013	-0,52402
Log. Numerat.	+0,6839588	-9,7193479
Log. Denom.	+2,2242038	-3,4129220
L. N	+8,4597550	+6,3064259
adde Log. $\frac{2(m+1)}{\mu}$	-0,9347258	+9,7062796
L. Pars II.	-9,3944808	+6,0127055
L. M	-0,4943689	-9,6357250
L. μ^2	+0,9848000	+3,4416924
L. P. I.	-9,5095689	-6,1940326
P. I.	-0,3232	-0,0002
- P. II.	+0,2480	-0,0001
N	-0,0752	-0,0003
at N	+0,0288	+0,0002

§. 543.

Pro partibus incognitis ponamus:

$$\begin{aligned} \mathfrak{B} = & \beta. \text{ cof. } (t + 2r) + \gamma. \text{ cof. } (2p - t - 2r) \\ & + \delta. \text{ cof. } (2p + t + 2r) \end{aligned}$$

$$\begin{aligned} \mathfrak{Z} = & b. \text{ fin. } (t + 2r) + c. \text{ fin. } (2p - t - 2r) \\ & + d. \text{ fin. } (2p + t + 2r) \end{aligned}$$

vnde quaeramus litteras \mathfrak{M} et \mathfrak{M}' :

Pro \mathfrak{M} .

$$\begin{array}{l} \mathfrak{B}(-9,221.\text{cof.}2p) \left| \begin{array}{l} \text{cof. } (t + 2r) \\ -4,6106.(\gamma + \delta) \end{array} \right| \begin{array}{l} \text{cof. } (2p - t - 2r) \\ -4,6106. \beta \end{array} \left| \begin{array}{l} \text{cof. } (2p + t + 2r) \\ -4,6106. \beta \end{array} \right. \\ \mathfrak{B}(+0,026.) \left| \begin{array}{l} +0,0264. \beta \\ +0,0264. \gamma \end{array} \right| \begin{array}{l} +0,0264. \gamma \\ +0,0264. \delta \end{array} \left| \begin{array}{l} +0,0264. \delta \\ +0,0264. \delta \end{array} \right. \\ \mathfrak{Z}(-3,990.\text{fin.}2p) \left| \begin{array}{l} -1,9953.(c + d) \\ -1,9953. b \end{array} \right| \begin{array}{l} -1,9953. b \\ -1,9953. b \end{array} \left| \begin{array}{l} -1,9953. b \\ -1,9953. b \end{array} \right. \end{array}$$

Pro \mathfrak{M}' .

$$\begin{array}{l} \mathfrak{B}(-3,990.\text{fin.}2p) \left| \begin{array}{l} \text{fin. } (t + 2r) \\ -1,9953.(\gamma - \delta) \end{array} \right| \begin{array}{l} \text{fin. } (2p - t - 2r) \\ -1,9953. \beta \end{array} \left| \begin{array}{l} \text{fin. } (2p + t + 2r) \\ -1,9953. \beta \end{array} \right. \\ \mathfrak{Z}(+5,360.\text{cf } 2p) \left| \begin{array}{l} -2,6803.(c - d) \\ -2,6803. b \end{array} \right| \begin{array}{l} -2,6803. b \\ +2,6803. b \end{array} \left| \begin{array}{l} +2,6803. b \\ +2,6803. b \end{array} \right. \\ \mathfrak{Z}(-0,0272) \left| \begin{array}{l} -0,0272. b \\ -0,0272. c \end{array} \right| \begin{array}{l} -0,0272. c \\ -0,0272. d \end{array} \left| \begin{array}{l} -0,0272. d \\ -0,0272. d \end{array} \right. \end{array}$$

§. 544.

Iam calculum litterarum \mathcal{N}' et \mathcal{N} incipiamus
ab angulo $2p - t - 2r$:

	β	b	γ	c
Log. M'	- 0,3000187	- 0,4281870		- 8,4351545
$L. \frac{2(m+1)}{\mu}$	- 0,9347258	- 0,9347258		- 0,9347258
$L. \frac{2(m+1)M'}{\mu}$	+ 1,2347445	+ 1,3629128		+ 9,3698803
$\frac{2(m+1)M'}{\mu}$	+ 17,1690	+ 23,0629		+ 0,2343
- \mathcal{M}'	+ 4,6106	+ 1,9953	- 0,0264	
Num.	+ 21,7796	+ 25,0582	- 0,0264	+ 0,2343
L. Num.	+ 1,3380498	+ 1,3989498	- 8,4216039	+ 9,3698803
L. Den.	+ 2,2242038	+ 2,2242038	+ 2,2242038	+ 2,2242038
L. \mathcal{N}'	+ 9,1138460	+ 9,1747460	- 6,1974001	+ 7,1456765
$L. \frac{2(m+1)}{\mu}$	- 0,9347258	- 0,9347258	- 0,9347258	- 0,9347258
L. P. II.	- 0,0485718	- 0,1094718	+ 7,1321259	- 8,0804023
L. M'	- 0,3000187	- 0,4281870		- 8,4351545
L. μ^2	+ 0,9848000	+ 0,9848000		+ 0,9848000
L. P. I.	- 9,3152187	- 9,4433870		- 7,4503545
P. I.	- 0,2066	- 0,2776		- 0,0028
- P. II.	+ 1,1183	+ 1,2867	- 0,0014	+ 0,0120
\mathcal{N}'	+ 0,9117	+ 1,0091	- 0,0014	+ 0,0092
at \mathcal{N}	+ 0,1300	+ 0,1495	- 0,0002	+ 0,0014

hinc

$$\gamma = +0,0288 + 0,1300 \beta + 0,1495 b - 0,0002 \gamma + 0,0014 c$$

$$c = -0,0752 + 0,9117 \beta + 1,0091 b - 0,0014 \gamma + 0,0092 c$$

vnde

vnde concludimus

$$\gamma = +0,0287 + 0,1313. \beta + 0,1509. b$$

$$c = -0,0757 + 0,9199. \beta + 1,0182. b.$$

§. 545.

Pro tertio angulo binas columnas δ et d prae-
termittamus, vnde calculus erit :

Pro angulo $2p + t + 2r$

	β	b
Log. M'	- 0,3000187	+ 0,4281870
$L. \frac{2(m+1)}{\mu}$	+ 9,7062796	+ 9,7062796
$L. \frac{2(m+1)M'}{\mu}$	- 0,0062983	+ 0,1344666
$L. \frac{2(m+1)M'}{\mu}$	- 1,0146	+ 1,3629
- M'	+ 4,6106	+ 1,9953
Numer.	+ 3,5960	+ 3,3582
L. Num.	+ 0,5558197	+ 0,5261066
L. Den.	- 3,4129200	- 3,4129220
Log. N'	- 7,1428977	- 7,1131846
$L. \frac{2(m+1)}{\mu}$	+ 9,7062796	+ 9,7062796
L. P. II.	- 6,8491773	- 6,8194642
Log M'	- 0,3000187	+ 0,4281870
Log μ^2	+ 3,4416924	+ 3,4416924
L. P. I.	- 6,8583263	+ 6,9864946
P. I.	- 0,0007	+ 0,0009
- P. II.	+ 0,0007	+ 0,0007
N'	- 0,0000	+ 0,0016
N'	- 0,0014	- 0,0013

D d d d 3

hinc

hinc

$$\delta = + 0,0002 - 0,0014. \beta - 0,0013. b$$

$$d = - 0,0003 - 0,0000. \beta + 0,0016. b.$$

§. 546.

Quum igitur nunc habeamus :

$$\gamma + \delta = + 0,0289 + 0,1299. \beta + 0,1496. b$$

$$\gamma - \delta = + 0,0285 + 0,1327. \beta + 0,1522. b$$

$$c + d = - 0,0760 + 0,9199. \beta + 1,0198. b$$

$$c - d = - 0,0754 + 0,9199. \beta + 1,0166. b$$

reperiemus pro angulo primo $t + 2r$

$$\mathfrak{N} = - 6,73498 - 2,42600. \beta - 2,72476. b$$

$$\mathfrak{M} = - 0,30032 - 2,73042. \beta - 3,05575. b.$$

§. 547.

§. 547.

Iam igitur pro prima columna sequens instituat-
tur calculus :

Pro angulo $t + 2r$.

	i .	β	b
L. M	- 9,4775843	- 0,4362295	- 0,4851178
$L_{\frac{2(m+1)}{\mu}}$	+ 9,9823746	+ 9,9823746	+ 9,9823746
$L_{\frac{2(m+1)}{\mu}} M$	- 9,4599589	- 0,4186041	- 0,4674924
$\frac{2(m+1)}{\mu} M$	- 0,28837	- 2,62183	- 2,93422
- \mathcal{M}	+ 6,73498	+ 2,42600	+ 2,72476
Numer.	+ 6,44661	- 0,19583	- 0,20946
L. Num.	+ 0,8093314	- 9,2918792	- 9,3211011
L. Den.	- 2,7767879	- 2,7767879	- 2,7767879
Log. \mathcal{N}	- 8,0325435	+ 6,5150913	+ 6,5443132
$L_{\frac{2(m+1)}{\mu}}$	+ 9,9823746	+ 9,9823746	+ 9,9823746
L. P. II	- 8,0149181	+ 6,4974659	+ 6,5266878
Log M	- 9,4775843	- 0,4362295	- 0,4851178
Log. μ^2	+ 2,8895024	+ 2,8895024	+ 2,8895024
L. P. I.	- 6,5880819	- 7,5467271	- 7,3746202
P. I	- 0,0004	- 0,0035	- 0,0024
- P. II	+ 0,0103	- 0,0003	- 0,0003
N	+ 0,0099	- 0,0038	- 0,0027
\mathcal{N}	- 0,0108	+ 0,0003	+ 0,0004

hinc

hinc $\beta = -0,0108 + 0,0003. \beta + 0,0004. b$

et $b = +0,0099 - 0,0038. \beta - 0,0027. b$

ex priori fit $\beta = -0,0108 + 0,0004. b$

vnde $b = +0,0099 - 0,0027. b$; ideoque

$b = +0,0099$; $\beta = -0,0108$;

$\gamma = +0,0288$; $c = -0,0755$;

$\delta = +0,0001$; $d = -0,0004$;

vnde tertia euolutio nobis praebet

$$\mathfrak{B} = -0,0108. \cos.(t+2r) + 0,0288. \cos.(2p-t-2r) \\ + 0,0001. \cos.(2p+t+2r)$$

$$Z = +0,0099. \sin.(t+2r) - 0,0755. \sin.(2p-t-2r) \\ - 0,0004. \sin.(2p+t+2r).$$

§. 548.

Completi ergo valores nostrarum litterarum \mathfrak{B}
et Z erunt:

$$\mathfrak{B} = +0,0098. \cos. t - 0,0584. \cos.(2p-t) \\ + 0,0220. \cos.(2p+t)$$

$$+ 0,0189. \cos.(t-2r) - 0,0017. \cos.(2p-t+2r) \\ - 0,0096. \cos.(2p+t-2r)$$

$$- 0,0108. \cos.(t+2r) + 0,0288. \cos.(2p-t-2r) \\ + 0,0001. \cos.(2p+t+2r)$$

$$Z = -0,2496. \sin. t + 0,0697. \sin.(2p-t)$$

$$- 0,0247. \sin.(2p+t)$$

$$+ 0,0204. \sin.(t-2r) + 0,0017. \sin.(2p-t+2r)$$

$$+ 0,1016. \sin.(2p+t-2r)$$

$$+ 0,0099. \sin.(t+2r) - 0,0755. \sin.(2p-t-2r)$$

$$- 0,0004. \sin.(2p+t+2r).$$

NOVAE